

0. [1] True/False (Assign True to True statements; assign false otherwise)

- a. For every DFA, there is an NFA. **True**
- b. For every  $\Sigma^*$ , there is a DFA. **True**

1. [1] Multiple Choice/single answer (select the best answer):

1.1 For every Deterministic Finite Automaton **D** .

- A. there is an infinite language
- B. there is a finite language
- C. there is a regular expression that cannot be defined by a CFG
- D. there is a Non-deterministic Finite Automaton (NFA)
- E. there is a non-regular language
- F. A and C.
- G. B and C
- H. A and E

1.2  $L = \{ c^n d^* h^* b^* a^n d^* : \text{where } n > 0 \}$  is a set of strings that **H**

- A. includes ccddhbbbaadd
- B. includes cccdddhbbbaaadd
- C. includes cccdddhbbbaadddd
- D. can be accepted by an NFA
- E. can be defined by a CFG
- F. All of the above
- G. A & E
- H. A, B & E
- I. A & D
- J. B & E

2. [2] Write a CFG for  $L_2 = \{ d^* c^n f j^n b^* d : \text{where } n > 0 \}$

**CFG:**

**S**  $\rightarrow$  **DXBd**

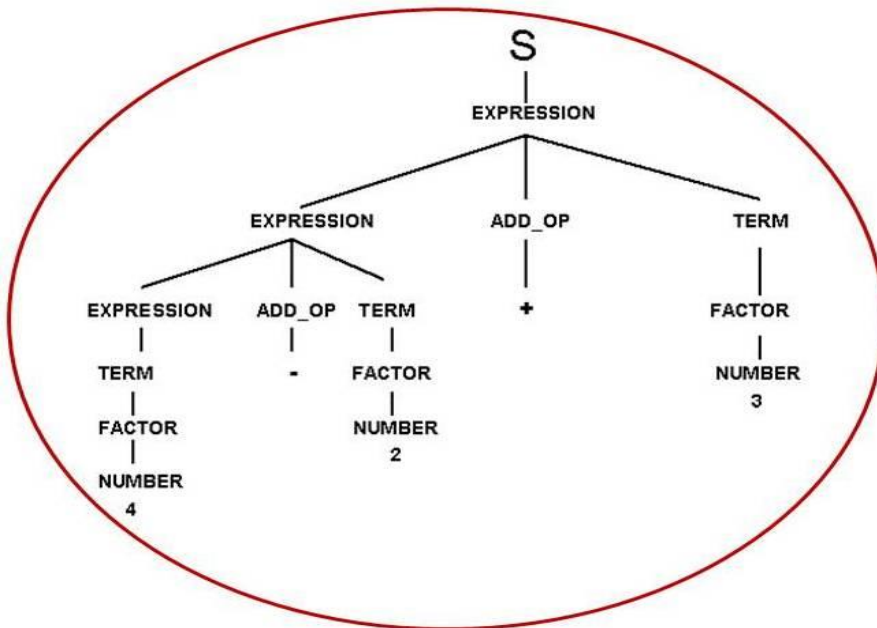
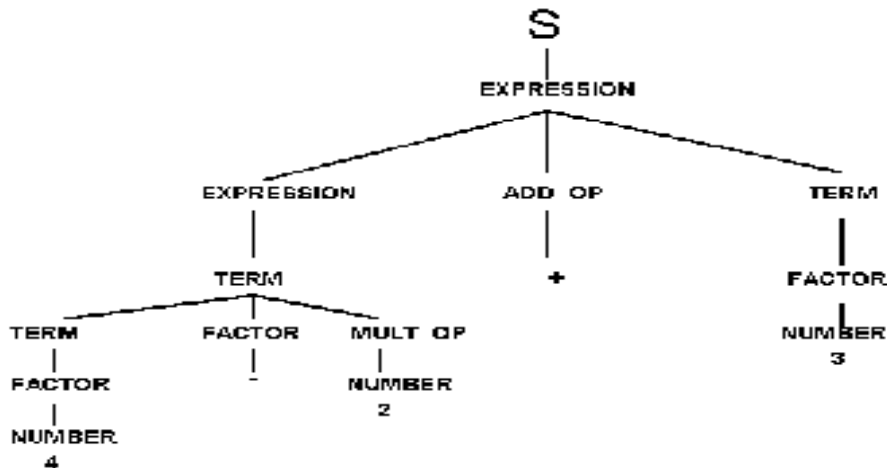
**D**  $\rightarrow$  **dD** | **^**

**X**  $\rightarrow$  **cXj** | **cfj**

**B**  $\rightarrow$  **bB** | **^**

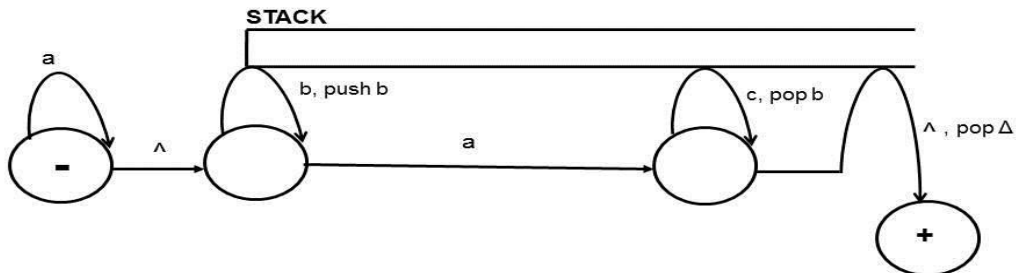
3. [1] Which of the parse trees is generated by the following CFG (Context-Free Grammar)? Select the correct parse tree (by circling the tree or writing “answer” next to the tree).

$S \rightarrow \text{STATEMENT} \mid \text{EXPRESSION}$   
 $\text{STATEMENT} \rightarrow \text{IDENTIFIER ASSIGN\_OP EXPRESSION}$   
 $\text{EXPRESSION} \rightarrow \text{TERM} \mid \text{EXPRESSION ADD\_OP TERM} \mid (\text{EXPRESSION})$   
 $\text{TERM} \rightarrow \text{FACTOR} \mid \text{TERM MULT\_OP FACTOR} \mid (\text{EXPRESSION})$   
 $\text{FACTOR} \rightarrow \text{IDENTIFIER} \mid \text{NUMBER} \mid - \text{FACTOR} \mid (\text{EXPRESSION})$   
 $\text{ADD\_OP} \rightarrow + \mid -$   
 $\text{ASSIGN\_OP} \rightarrow =$   
 $\text{MULT\_OP} \rightarrow * \mid /$   
 $\text{NUMBER} \rightarrow 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \dots$

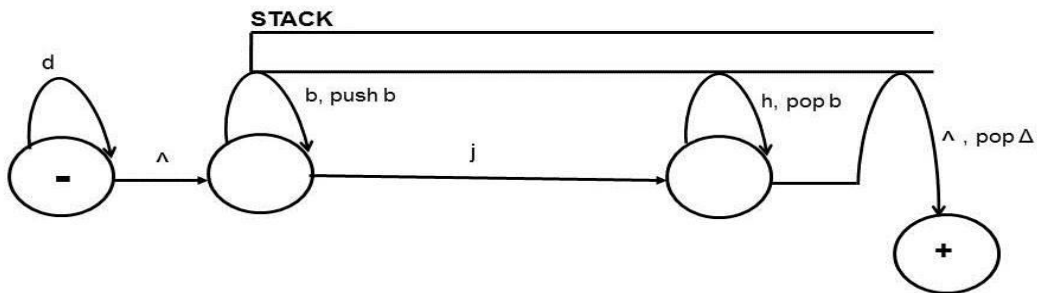


4. [1] Draw a PDA or One-Stack Automaton for  $L_4 = \{ a^*b^nac^n : \text{where } n \geq 0 \}$   
or  $= \{ d^*b^nh^n : \text{where } n \geq 0 \}$

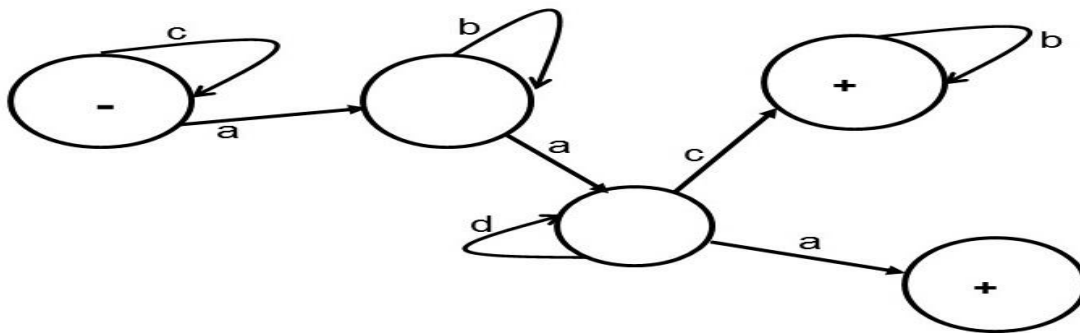
One-Stack Automaton for  $\{ a^*b^nac^n : \text{where } n \geq 0 \}$



One-Stack Automaton for  $\{ d^*b^nh^n : \text{where } n \geq 0 \}$



5. [1] Write the regular expression for the following NFA.



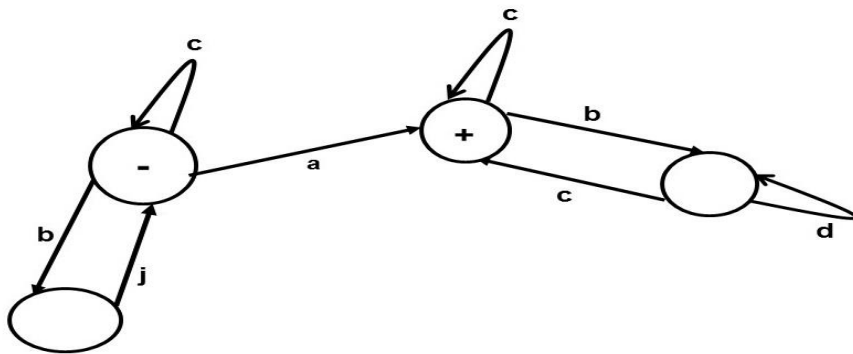
**$c^*ab^*ad^*a + c^*ab^*ad^*cb^*$**

6. [1] Write a CFG for  $L_6 = \{ d^*a^ncb^nd^* : \text{where } n > 1 \}$

**CFG:**

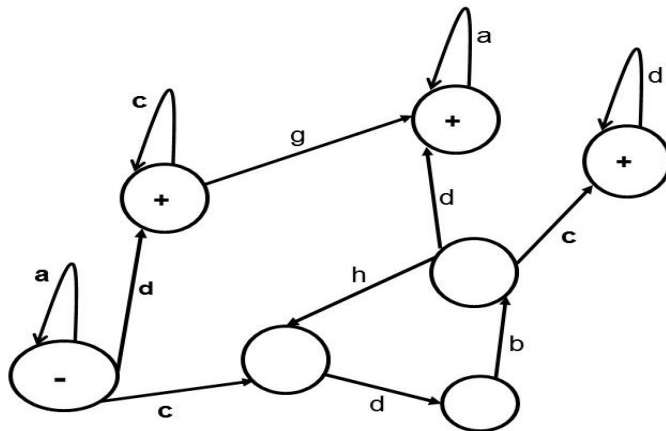
**$S \rightarrow DXD$   
 $D \rightarrow dD \mid \wedge$   
 $X \rightarrow aXb \mid aacbb$**

7a. [2] Write the regular expression for the following NFA.



$(c+bj)^* a (c+bd^*c)^*$

7b. [2] Write the regular expression for the following NFA



$a^*dc^* + a^*dc^*ga^* + a^*c(dbh)^*db(hdb)^*da^* + ac(dbh)^*db(hdb)^*cd^*$

8. [2] Write a CFG for  $L_8 = \{ a^*c^ndedh^nd^*a^* : \text{where } n > 1 \}$

$S \rightarrow AXDA$

$A \rightarrow aA \mid \wedge$

$D \rightarrow dD \mid \wedge$

$X \rightarrow cXh \mid ccdedhh$

9. [2] Write a CFG for  $L_9 = \{ a^n d^n g h b^m c^m : \text{where } n > 0, m > 1 \}$

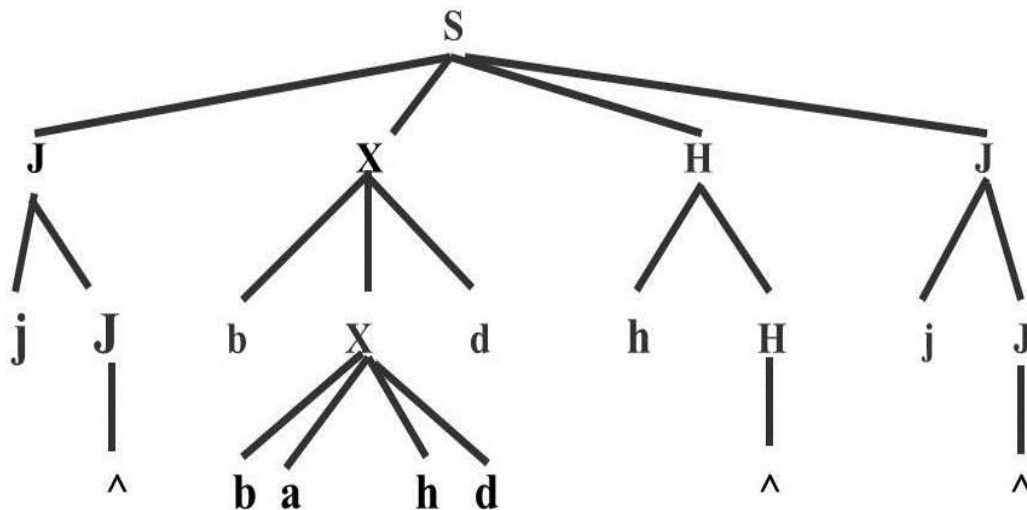
$S \rightarrow XghY$   
 $X \rightarrow aXd \mid ad$   
 $Y \rightarrow bYc \mid bbcc$

10. [2] Write a CFG for  $L_{10} = \{ j^* b^n a h d^n h^* j^* : \text{where } n > 0 \}$   
and give a parse tree for jbbahddhj

CFG:

$S \rightarrow JXHJ$   
 $J \rightarrow jJ \mid \wedge$   
 $X \rightarrow bXd \mid bahd$   
 $H \rightarrow hH \mid \wedge$

A parse tree for jbbahddhj



11. [2] Draw a PDA or One-Stack Automaton for  $L_{11} = \{ d^*ca^ncd^*j^nb^* : \text{where } n > 0 \}$

